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| Module code | SM-4322 | | |
| Module Title | Functional Analysis | | |
| Degree/Diploma | Bachelor of Science (Mathematics) | | |
| Type of Module | Major Option | | |
| Modular Credits | 4 | Total student Workload | 10 hours/week |
| | | Contact hours | 4 hours/week |
| Prerequisite | SM-4327 Real Analysis | | |
| Anti-requisite | None | | |
| Aims | | | |
| To learn properties of general mathematical objects with algebraic and topological structures. | | | |
| Learning Outcomes | | | |
| <i>On successful completion of this module, a student will be expected to be able to:</i> | | | |
| Lower order : | 40% | - understand basic concepts and tools of functional analysis and use them in applications | |
| Middle order : | 40% | - use general approach to some structures in real and complex analysis | |
| Higher order: | 20% | - understand main algebraic structures and use their properties | |
| Module Contents | | | |
| <ul style="list-style-type: none"> - Metrics and metric spaces. Subspaces. Open and closed sets in metric spaces. - Convergence of sequences. Cauchy sequences and completeness. Normed spaces. Banach spaces. - Spaces of sequences. Function spaces with supremum norm. Finite dimensional spaces. - Linear operators. Boundedness and continuity. Spaces of linear operators. Linear functionals. The dual space. Hahn-Banach theorem with examples and applications. - Inner product spaces. Hilbert spaces. Orthogonality in Hilbert spaces. Best approximation. - Orthogonal complements. Direct sum. Orthonormal sets and sequences. The dual of a Hilbert space. | | | |
| Assessment | Formative assessment | Tutorial and feedback. | |
| | Summative assessment | Examination: 60% Coursework: 40% - 1 class test (20%) - 1 assignment (20%) | |